

Temperature and Pressure Dependence of the Viscosity of the Ionic Liquids 1-Methyl-3-octylimidazolium Hexafluorophosphate and 1-Methyl-3-octylimidazolium Tetrafluoroborate

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The viscosities of the ionic liquids 1-methyl-3-octylimidazolium hexafluorophosphate, [OMIM]PF₆, and 1-methyl-3-octylimidazolium tetrafluoroborate [OMIM]BF₄, have been measured between (0 and 80) °C and at pressures to 176 MPa ([OMIM]PF₆) and 224 MPa ([OMIM]BF₄) with a falling-body viscometer. The overall uncertainty is estimated at ± (2 to 3) %. Modified Litovitz and Vogel–Fulcher–Tammann equations are used to represent the temperature and pressure dependence. The T_0 parameter for the latter is found to be consistent with Angell's relationship linking T_0 and the strength parameter D with the glass temperature T_g . Densities between (0 and 90) °C at atmospheric pressure are also reported for both substances. These have an overall uncertainty estimated at ± 0.00005 g·cm⁻³. The in-built viscosity correction for the Anton-Paar DMA5000 densimeter was confirmed using high-viscosity reference standards to an upper limit of 16 Pa·s.

Introduction

This work continues a series on the transport properties of ionic liquids at high pressure. There is currently great interest in ionic liquids for their favorable solvent and electrochemical properties; their potential, in favorable circumstances, as replacements for traditionally used industrial organic solvents; and their use in biphasic catalysis and the electro-winning of metals.¹ Hence it is important that reliable thermophysical data and property databases of these materials be available for efficient design of processes and plant. Despite (or perhaps because of) the complex interactions (electrostatic, van der Waals, and H-bonding) between the component ions, ionic liquids are also of interest in the development of theoretical models of electrolytes as the liquid region is much more readily accessible to experiment than for simple inorganic salts. Determination of the transport properties (viscosity, ionic conductivity, and ion self-diffusion coefficients) allows analysis of correlations between ionic velocities, and it is important that the measurements be precise and accurate. High-pressure data, in principle, allow the separation of volume effects from those of temperature. This paper forms one element of a program of systematic thermophysical property measurements for representative ionic liquids.

Here we report viscosities for two members of one of the most commonly studied ionic liquid groups, that based on imidazolium-containing cations, namely, 1-methyl-3-octylimidazolium hexafluorophosphate ([OMIM]PF₆ or [C₈-mim]PF₆) and 1-methyl-3-octylimidazolium tetrafluoroborate ([OMIM]BF₄ or [C₈-mim]BF₄). The choice has also been influenced by the availability of pVT data necessary for measurements made with a falling-body viscometer. These new measurements supplement our earlier ones on 1-butyl-3-methylimidazolium hexafluoro-

phosphate ([BMIM]PF₆ or [C₄-mim]PF₆),² allowing the comparison of pairs of ionic liquids with either a common cation ([OMIM]⁺) or a common anion (PF₆⁻). Densities were also measured at atmospheric pressures with an Anton-Paar DMA5000 vibrating tube densimeter, and we have tested the range of validity of the viscosity correction for this instrument, extending it to 16 Pa·s.

Experimental Section

Two separate [OMIM]PF₆ samples (designated OP1 and OP2 in the tables) and one of [OMIM]BF₄ (sample OB1) were prepared in a manner similar to [BMIM]PF₆.³ Care was taken to remove chloride: any residual amount was less than the detection limit of elemental titration analysis (mass fraction 10⁻⁴). The molar masses were taken as (340.289 and 282.129) g·mol⁻¹, respectively.

Imidazolium-containing ionic liquids are hygroscopic, and as with most ionic liquids, the physical properties are very sensitive to the presence of small amounts of water.^{3–6} These liquids, particularly the hexafluorophosphates, can attack glass at temperatures above 70 °C in the presence of traces of water. Hence we have taken care to minimize exposure to water in handling the samples. The water contents of OP2 and OB1 were determined by Karl Fischer titration to be ((27 ± 4) and (54 ± 10)·10⁻⁶) mass fraction, respectively, prior to their vacuum sealing in glass ampules and their shipment from Sendai to Canberra where the density and viscosity measurements were made. The water contents of OP1 and the [BMIM]PF₆ sample reported on previously,² though not measured, are estimated to lie within the same range. The ionic liquid ampules were warmed to about 75 °C to increase the sample fluidity and opened inside a glovebox with the atmosphere dried with either phosphorus pentoxide or concentrated sulfuric acid. The oven-dried viscometer sample tube was then filled and sealed within the glovebox. The sample tube was then inserted into the pressure vessel. Contrary to our usual practice, the ionic liquids

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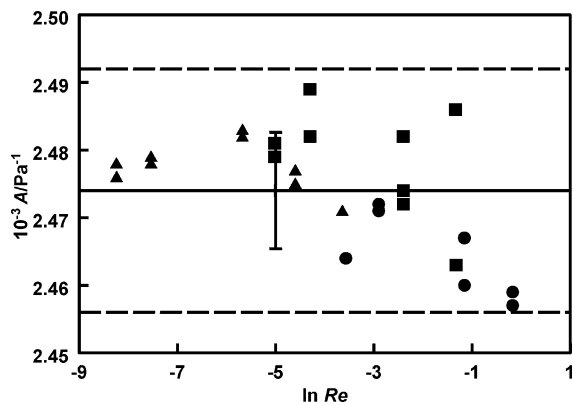


Figure 1. Viscometer calibration constant, A , for Cannon certified reference oils, (20 to 50) °C. $A = (2.474 \pm 0.009) 10^3 \text{ Pa}^{-1}$. Symbols: ●, N100; ■, S200; and ▲, N1000. The dashed lines represent the expanded uncertainty of fit or 95 % confidence limits.

Table 1. Test of the Viscosity Correction for the Anton-Paar DMA5000 Densimeter Using Cannon Reference Fluid N4000

θ °C	η mPa·s	ρ_{uncorr} g·cm ⁻³	ρ_{corr}^a g·cm ⁻³	$\rho_{\text{uncorr}} - \rho_{\text{corr}}$ g·cm ⁻³	ρ^b g·cm ⁻³
20	16 174	0.883 99	0.883 37	0.000 17	0.8832 ± 0.0002
25	10 242	0.881 17	0.880 56	0.000 16	0.8804 ± 0.0002
40	2 966	0.872 74	0.872 13	0.000 13	0.8720 ± 0.0002
50	1 444	0.867 15	0.866 54	0.000 14	0.8664 ± 0.0002
60	756	0.861 55	0.860 95	0.000 15	0.8608 ± 0.0001

^a Uncertainty ± 0.000 05 g·cm⁻³. ^b As given by Cannon.

Table 2. Parameters for Tait (\ln form) and Hayward Equations of State

	[OMIM]BF ₄		[OMIM]PF ₆	
$T/^\circ\text{C}$	25	50	25	50
B/MPa	125.22	90.62	183.84	190.58
C	0.062 20	0.054 45	0.081 33	0.093 56
$\delta\rho/\%$ ^a	0.2	0.1	0.1	0.1
	[OMIM]BF ₄		[OMIM]PF ₆	
α_{00}/MPa	-1618.54		-445.350	
$\alpha_{01} \times 10^3/(\text{MPa}\cdot\text{K})$	1091.09		817.894	
α_{10}	10.6362		-4.616 60	
α_{11}/K	-1172.86		2935.64	
$\delta\rho/\%$ ^a	0.1		0.1	

^a Standard uncertainty of fit to the density.

were not filtered during the filling of the viscometer due to the possibility of reaction with the glass sinter at the loading temperature; however, filtration is part of the preparation procedure.³

The falling body viscometer employed and its operation have been described previously.² The working equation is

$$\eta(p, T) = \frac{t(1 - \rho/\rho_s)}{A[(1 + 2\alpha(T - T_{\text{ref}})][1 - 2\beta(p - p_{\text{ref}})/3]} \quad (1)$$

where η is the shear viscosity, t is the fall time, ρ is the density of the fluid, ρ_s is the density of the sinker, α is the coefficient of thermal expansion, and β is the bulk compressibility of the sinker and tube material, in this case 316 stainless steel. A is the calibration constant. The sinker densities were corrected for changes in T and p from the reference state point, $T_{\text{ref}} = 298.15$ K and $p_{\text{ref}} = 0.1$ MPa using the relation:

$$\rho_s = \frac{\rho_s(T_{\text{ref}}, p_{\text{ref}})}{[1 + 3\alpha(T - T_{\text{ref}})][1 - \beta(p - p_{\text{ref}})]} \quad (2)$$

Table 3. Density ρ of [OMIM]BF₄ from $\theta = (0 \text{ to } 90)^\circ\text{C}$

$\theta/^\circ\text{C}$	$\rho/\text{g}\cdot\text{cm}^{-3}$	$\theta/^\circ\text{C}$	$\rho/\text{g}\cdot\text{cm}^{-3}$	$\theta/^\circ\text{C}$	$\rho/\text{g}\cdot\text{cm}^{-3}$	$\theta/^\circ\text{C}$	$\rho/\text{g}\cdot\text{cm}^{-3}$
0	1.120 96	20	1.107 11	40	1.093 37	80	1.066 60
5	1.117 48	20	1.107 11	50	1.086 56	90	1.060 08
10	1.114 01	25	1.103 68	60	1.079 83		
15	1.110 55	30	1.100 24	70	1.073 18		

Table 4. Density ρ of [OMIM]PF₆ from $\theta = (0 \text{ to } 90)^\circ\text{C}$

$\theta/^\circ\text{C}$	$\rho/\text{g}\cdot\text{cm}^{-3}$	$\theta/^\circ\text{C}$	$\rho/\text{g}\cdot\text{cm}^{-3}$
Sample OP1			
0	1.256 13	40	1.225 34
5	1.252 25	50	1.217 70
10	1.248 38	60	1.210 29
15	1.244 52	70	1.202 88
20	1.240 68	80	1.195 49
25	1.236 84	90	1.188 13
30	1.233 01		
Sample OP2			
25	1.236 75	50	1.217 68

The viscometer tube diameter is 6.52 mm, and that of the sinker is 6.0 mm. The Reynolds number for annular flow in a viscometer of this type is given by

$$Re = 2r_1^2 \rho v / ((r_2 - r_1)\eta) \quad (3)$$

where v is the terminal velocity of the sinker and r_1 and r_2 are the radii of the sinker and tube, respectively.

The previous calibration² was extended using Cannon viscosity standards N100, S200, and N1000 (Lot Nos. 03501, 04201,

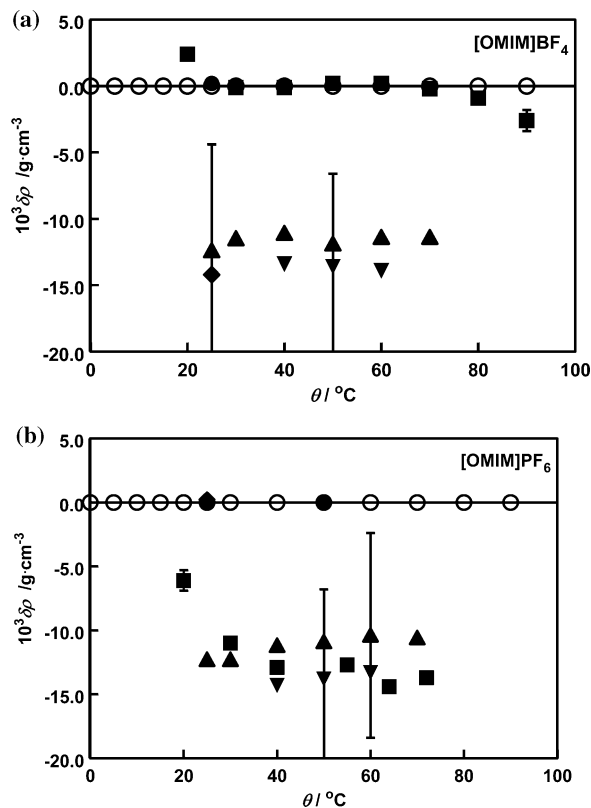


Figure 2. (a) Residuals (experimental - calculated values) for the fit of the experimental atmospheric pressure and literature densities for [OMIM]BF₄ to eq 6a as a function of temperature, θ . Symbols: ○, this work; ▲, ref 7; ▼, ref 10; ■, ref 11; ◆, ref 12; ●, ref 13. (b) Residuals (experimental - calculated values) for the fit of the experimental atmospheric pressure and literature densities for [OMIM]PF₆ to eq 6b as a function of temperature, θ . Symbols: ○, this work, sample OP1; ●, this work, sample OP2; ▲, ref 7; ▼, ref 10; ■, ref 11; ◆, ref 14.

Table 5. Viscosity η of [OMIM]BF₄ from $\theta = (0 \text{ to } 80)^\circ\text{C}$ and $p = (0.1 \text{ to } 224) \text{ MPa}$

θ	t	p	V	ρ	η	Re	θ	t	p	V	ρ	η	Re
$^\circ\text{C}$	s	MPa	$\text{cm}^3\cdot\text{mol}^{-1}$	$\text{g}\cdot\text{cm}^{-3}$	mPa·s		$^\circ\text{C}$	s	MPa	$\text{cm}^3\cdot\text{mol}^{-1}$	$\text{g}\cdot\text{cm}^{-3}$	mPa·s	
0.00	6691	0.1	251.68	1.12096	2291	0.0005	50.00	258.1	0.1	259.65	1.08656	88.7	0.33
0.00	6686	0.1	251.68	1.12096	2289	0.0005	50.00	259.7	0.7	259.57	1.08689	89.2	0.32
5.00	4313	0.1	252.47	1.11748	1477	0.0012	50.00	272.3	4.9	259.01	1.08925	93.5	0.30
5.00	4314	0.1	252.47	1.11748	1478	0.0012	50.00	289.3	10.5	258.29	1.09228	99.3	0.26
10.00	2868	0.1	253.25	1.11401	982	0.0027	50.00	340.1	25.8	256.39	1.01271	118.2	0.17
10.00	2867	0.1	253.25	1.11401	982	0.0027	50.00	438.8	50.8	253.52	1.11283	150.1	0.12
15.00	1964	0.1	254.04	1.11055	673	0.0058	50.00	560.0	75.7	250.91	1.12441	191.2	0.073
15.00	1964	0.1	254.04	1.11055	673	0.0058	50.00	709.2	100.6	248.52	1.13522	241.8	0.046
20.00	1381	0.1	254.83	1.10711	473	0.012	50.00	890.6	125.5	246.33	1.14530	303.1	0.029
20.00	1380	0.1	254.83	1.10711	473	0.012	50.00	1108	149.9	244.36	1.15456	376.5	0.019
25.00	994.6	0.1	255.63	1.10368	341	0.023	50.00	1384	175.5	242.44	1.16371	469.8	0.012
25.00	1147	11.2	254.29	1.10948	393.0	0.017	50.00	1703	199.8	240.75	1.17188	577.3	0.008
25.00	1390	26.2	252.61	1.11683	475.7	0.012	60.00	168.2	0.1	261.27	1.07983	57.8	0.77
25.00	1868	50.5	250.21	1.12756	638.3	0.007	60.00	168.2	0.1	261.27	1.07983	57.8	0.77
25.00	1890	51.5	250.12	1.12798	645.9	0.006	60.00	187.6	10.8	259.65	1.08655	64.4	0.62
25.00	2109	60.8	249.29	1.13173	720.1	0.0052	60.00	217.5	25.7	257.64	1.09506	74.6	0.47
25.00	2646	80.2	247.68	1.13907	902.3	0.0033	60.00	275.4	50.3	254.76	1.10743	94.3	0.30
25.00	3317	100.2	246.19	1.14596	1130	0.0021	60.00	347.4	75.6	252.28	1.11829	118.7	0.19
25.00	3993	116.7	245.07	1.15121	1359	0.0015	60.00	433.0	100.5	250.21	1.12755	147.7	0.12
25.00	4027	117.5	245.02	1.15147	1371	0.0014	60.00	535.7	125.3	248.43	1.13564	182.5	0.080
30.00	732.0	0.1	256.42	1.10024	251	0.041	60.00	658.9	150.2	246.88	1.14276	224.3	0.054
30.00	730.2	0.1	256.42	1.10024	251	0.042	60.00	806.8	175.1	245.52	1.14911	274.4	0.036
35.00	549.0	0.1	257.23	1.09678	188.4	0.073	60.00	983.5	200.0	244.31	1.15478	334.1	0.024
35.00	548.4	0.1	257.23	1.09678	188.2	0.074	70.00	114.5	0.1	262.89	1.07318	39.4	1.6
35.00	548.8	0.1	257.23	1.09678	188.3	0.073	75.00	95.4	0.1	263.70	1.06990	32.8	2.4
35.00	549.9	0.1	257.23	1.09678	188.7	0.073	75.00	95.2	0.3	263.66	1.07004	32.7	2.4
35.00	549.2	0.1	257.23	1.09678	188.5	0.073	75.00	96.4	1.6	263.44	1.07095	33.2	2.3
35.00	553.9	0.8	257.13	1.09721	190.1	0.072	75.00	97.9	3.1	263.18	1.07201	33.7	2.3
35.00	568.1	2.9	256.86	1.09838	194.9	0.069	75.00	99.9	5.4	262.80	1.07353	34.4	2.2
35.00	586.5	5.6	256.51	1.00281	204.3	0.058	75.00	104.6	10.2	262.03	1.07672	36.0	2.0
35.00	624.7	10.9	255.84	1.10276	214.2	0.057	75.00	120.7	25.6	259.74	1.08619	41.4	1.5
35.00	744.9	26.0	254.06	1.11048	255.1	0.040	75.00	150.3	50.3	256.66	1.09923	51.5	1.0
35.00	986.1	50.7	251.50	1.12180	337.1	0.023	75.00	185.9	75.6	254.06	1.11048	63.6	0.65
35.00	1301	76.2	249.22	1.13205	444.0	0.014	75.00	227.6	100.5	251.91	1.11997	77.7	0.44
35.00	1676	100.3	247.35	1.14061	571.1	0.008	75.00	276.6	125.4	250.08	1.12815	94.3	0.30
35.00	2149	124.4	245.69	1.14829	731.7	0.005	75.00	335.7	150.4	248.50	1.13530	114.3	0.20
35.00	2781	150.2	244.13	1.15563	945.5	0.003	75.00	402.0	175.3	247.13	1.14160	136.8	0.14
35.00	4500	200.1	241.59	1.16779	1527	0.001	75.00	481.2	200.2	245.93	1.14717	163.6	0.10
40.00	419.7	0.1	258.03	1.09337	144.1	0.13	75.00	570.1	224.2	244.91	1.15198	193.7	0.07
50.00	258.3	0.1	259.65	1.08656	88.8	0.33	80.00	81.8	0.1	264.51	1.06660	28.1	3.2
50.00	258.1	0.1	259.65	1.08656	88.7	0.33							

and 05201p, respectively) over the temperature range of (20 to 50) $^\circ\text{C}$. These samples were filtered through a glass sinter (pore size (40 to 60) μm) prior to use. Excellent agreement within the experimental precision of 1 % was obtained, giving a calibration constant, $A = 2.474 \cdot 10^3 \text{ Pa}^{-1}$ (standard uncertainty $0.009 \cdot 10^3 \text{ Pa}^{-1}$) for the viscosity range of (51 to 2875) mPa·s and Reynolds number range of 0.0003 to 0.84 (see Figure 1).

Densities at atmospheric pressure were determined with an Anton-Paar DMA5000 vibrating-tube densimeter as described previously.² As before the glass vibrating-tube was carefully rinsed with filtered ethanol, acetone, and dry air before being loaded with ionic liquid. Previously we reported a test of the viscosity correction built in to the DMA5000 by using the Cannon reference fluid S200, which has a viscosity of 0.5848 Pa·s at 20 $^\circ\text{C}$.² We have extended this test by using Cannon N4000, viscosity 16.174 Pa·s at 20 $^\circ\text{C}$. The viscosity-corrected density agreed with that given by Cannon within the accuracy stated (Table 1). We believe this to be the most exacting test yet of the viscosity correction for this instrument.

Calculation of the viscosity from fall times requires knowledge of the density as a function of temperature and pressure. pVT data for [OMIM]BF₄ and [OMIM]PF₆ have been determined by Gu and Brennecke⁷ at (25 and 50) $^\circ\text{C}$. Gu and Brennecke fitted their data to the Tait equation of state but reported incorrect parameters. Corrected values are given in Table 2. As we needed again to extrapolate these pVT data to

higher temperatures, they were used to calculate the linear secant modulus

$$\kappa = V_0(p - p_0)/(V_0 - V) \quad (4)$$

as a function of temperature and pressure where V_0 is the molar volume at the saturation pressure p_0 for a given temperature T . κ was fitted to the Hayward-type equation:²

$$\kappa = (\alpha_{00} + \alpha_{10}/T) + (\alpha_{01} + \alpha_{11}/T)p \quad (5)$$

The coefficients α_{ij} are also given in Table 2. High-pressure densities needed for the viscosity measurements were then calculated using our atmospheric pressure densities and eqs 4 and 5. As the sinker is 5 to 7 times denser than the ionic liquids used in this study, it is sufficient if the density is known to better than 5 % for an overall uncertainty in the viscosity of 1 % as it enters the viscosity calculation (eq 1) in terms of the buoyancy factor $(1 - \rho/\rho_s)$. The uncertainty in densities estimated from eq 5 is probably of the order of ± 0.5 %.

These ionic liquids are readily supercooled, and our results for [OMIM]PF₆ probably extend into the supercooled region. This was the case for [BMIM]PF₆² where we were able to determine both the density at 0 $^\circ\text{C}$ and the viscosity at 25 $^\circ\text{C}$ to 174 MPa although the freezing points at (0.1 and 55) MPa are (11.85 and 23.0) $^\circ\text{C}$, respectively.⁸ The melting points of [OMIM]PF₆ and [OMIM]BF₄ do not appear to have been

Table 6. Viscosity η of [OMIM]PF₆ from $\theta = (0 \text{ to } 80)^\circ\text{C}$ and $p = (0.1 \text{ to } 176) \text{ MPa}$

θ °C	t s	p MPa	V cm ³ ·mol ⁻¹	ρ g·cm ⁻³	η mPa·s	Re	θ °C	t s	p MPa	V cm ³ ·mol ⁻¹	ρ g·cm ⁻³	η mPa·s	Re
Sample OP1													
50.00	470.4	0.1	279.45	1.2177	158	0.11	60.00	287.5	0.1	281.16	1.2103	96.8	0.30
50.00	470.0	0.1	279.45	1.2177	158	0.11	70.00	188.9	0.1	282.89	1.2029	63.6	0.69
50.00	473.1	0.1	279.45	1.2177	159	0.11	70.00	188.2	0.1	282.89	1.2029	63.4	0.70
50.00	474.0	0.1	279.45	1.2177	159	0.11	70.00	187.2	0.1	282.89	1.2029	63.1	0.71
50.00	660.7	26.3	276.13	1.2324	222	0.058	70.00	187.2	0.1	282.89	1.2029	63.1	0.71
50.00	881.5	49.9	273.42	1.2445	295	0.033	70.00	207.6	10.0	281.47	1.2090	69.8	0.58
50.00	1183	74.8	270.83	1.2565	395	0.019	80.00	128.6	0.1	284.64	1.1955	43.3	1.48
60.00	288.1	0.1	281.16	1.2103	97.0	0.30	80.00	128.8	0.1	284.64	1.1955	43.4	1.48
Sample OP2													
0.00	19144	0.1	270.90	1.2561	6410	0.0001	50.00	1210	76.0	270.70	1.2570	404	0.018
5.00	11608	0.1	271.74	1.2522	3889	0.0002	50.00	1573	99.7	268.46	1.2676	525	0.011
10.00	7277	0.1	272.58	1.2484	2439	0.0005	60.00	290.9	0.1	281.16	1.2103	97.9	0.29
20.00	3175	0.1	274.27	1.2407	1065	0.003	60.00	290.7	0.1	281.16	1.2103	97.8	0.29
25.00	2189	0.1	275.13	1.2368	734	0.005	60.00	291	0.1	281.16	1.2103	97.9	0.294
25.00	2180	0.1	275.13	1.2368	732	0.005	60.00	291	0.1	281.16	1.2103	97.8	0.295
25.00	2546	10.2	273.94	1.2422	854	0.004	60.00	343	13.5	279.33	1.2182	115	0.21
25.00	3108	24.6	272.35	1.2494	1041	0.003	60.00	419	30.3	277.19	1.2276	141	0.14
25.00	3884	39.9	270.75	1.2568	1299	0.002	60.00	526	50.4	274.80	1.2383	176	0.092
30.00	1547	0.1	275.98	1.2330	519	0.011	60.00	689	75.1	272.09	1.2507	230	0.055
35.00	1115	0.1	276.85	1.2291	375	0.020	60.00	901	100.4	269.56	1.2624	301	0.032
35.00	1104	0.1	276.85	1.2291	371	0.021	60.00	1163	125.2	267.28	1.2731	387	0.020
35.00	1204	5.5	276.18	1.2321	404	0.018	70.00	189.1	0.1	282.89	1.2029	63.7	0.69
35.00	1282	9.9	275.65	1.2345	430	0.015	70.00	240.9	21.3	279.93	1.2156	81.0	0.43
35.00	1585	25.6	273.83	1.2427	531	0.010	70.00	336.3	51.8	276.06	1.2327	113	0.23
35.00	2141	48.4	271.39	1.2539	716	0.006	70.00	414.5	72.9	273.64	1.2436	139	0.15
35.00	3020	74.9	268.81	1.2659	1008	0.003	70.00	546.9	100.3	270.74	1.2569	183	0.087
40.00	823.9	0.1	277.71	1.2253	277	0.037	70.00	701.3	125.9	268.27	1.2685	234	0.054
50.00	473.4	0.1	279.45	1.2177	159	0.11	70.00	890.2	148.8	266.23	1.2782	296	0.034
50.00	648.1	24.8	276.31	1.2315	217	0.060	70.00	1139	175.9	263.99	1.2890	378	0.021

Table 7. Coefficients of Best Fit for Equations 7 and 8

	coefficients and standard uncertainties	
	[OMIM]BF ₄	[OMIM]PF ₆
	Litovitz, eq 7	
ln(A/mPa·s)	-0.462 36 ± 0.004 15	-0.538 65 ± 0.006 00
$B \times 10^{-6}/\text{K}^3$	166.92 ± 0.11	189.29 ± 0.19
standard uncertainty of fit	0.5 %	0.7 %
	VFT, eq 8	
ln(A'/mPa·s)	-3.16 72 ± 0.030 4	-3.456 7 ± 0.053 8
B'/K	1283.52 ± 9.02	1407.98 ± 16.22
T_0/K	155.49 ± 0.51	158.03 ± 0.85
D^a	8.25	8.91
standard uncertainty of fit	0.3 %	0.6 %

^a Angell strength factor (B'/T_0).

determined as yet, although glass transition temperatures have been reported.⁹ Freezing behavior was observed in some of our viscosity runs with [OMIM]PF₆ (e.g., near 100 MPa at 25 °C). Attempts to determine the freezing line by NMR relaxation time experiments were unsuccessful, due in part to the apparent similarity of the T_1 relaxation times in the liquid and solid phases (both proton and fluorine) and hysteresis effects.

Results and Discussion

The density results at atmospheric pressure are presented in Tables 3 and 4 and can be represented by the polynomials

$$\rho([\text{OMIM}]\text{BF}_4)/\text{g}\cdot\text{cm}^{-3} = 1.121004 - 7.01436 \times 10^{-4} (\theta/^\circ\text{C}) + 2.66725 \times 10^{-7} (\theta/^\circ\text{C})^2 \quad (6a)$$

$$\rho([\text{OMIM}]\text{PF}_6)/\text{g}\cdot\text{cm}^{-3} = 1.256174 - 7.83151 \times 10^{-4} (\theta/^\circ\text{C}) + 3.03073 \times 10^{-7} (\theta/^\circ\text{C})^2 \quad (6b)$$

where θ is the Celsius temperature, with a standard uncertainty of (± 0.00003 and ± 0.00004) $\text{g}\cdot\text{cm}^{-3}$ respectively. Figure 2 shows deviations of literature density data^{7,10–14} for [OMIM]-

BF₄ and [OMIM]PF₆ from eqs 6. Error bars are given where the experimental precision is larger than the size of the symbols.

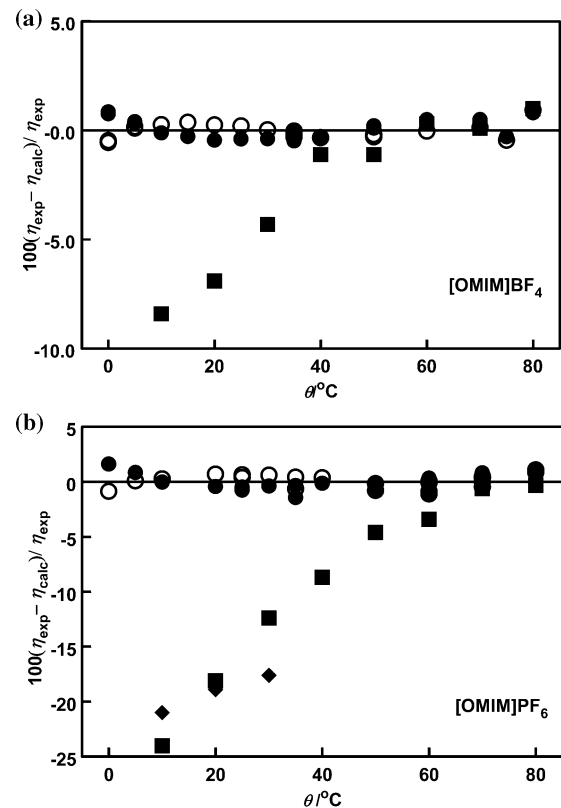


Figure 3. (a) Residuals (experimental - calculated values) for the fit of the experimental viscosities for [OMIM]BF₄ at atmospheric pressure to eqs 7 and 8 as a function of temperature, θ . Symbols: ●, this work, Litovitz eq 7; ○, this work, VFT eq 8; ■, ref 11. (b) Residuals (experimental - calculated values) for the fit of the literature viscosities for [OMIM]PF₆ at atmospheric pressure to eqs 7 and 8 as a function of temperature, θ . Symbols: ●, this work, Litovitz eq 7; ○, this work, VFT eq 8; ■, ref 11; ◆, ref 15.

Table 8. Coefficients of Best Fit for Equations 9, 10, and 11

	coefficients and standard uncertainties ^a		
	[OMIM]BF ₄	[OMIM]PF ₆	[BMIM]PF ₆
ML, eq 9			
<i>a</i>	-0.4585 ± 0.0035	-0.5344 ± 0.0062	-0.4061 ± 0.014
<i>b</i> × 10 ³ /MPa ⁻¹	2.7283 ± 0.055	4.7212 ± 0.273	2.354 ± 0.21
<i>c</i> × 10 ⁻⁶ /K ³	166.80 ± 0.10	189.107 ± 0.19	159.49 ± 0.43
<i>d</i> × 10 ⁻⁶ /(K ³ ·MPa ⁻¹)	0.2657 ± 0.0017	0.2696 ± 0.0083	0.3167 ± 0.0068
<i>e</i> /(K ³ ·MPa ²)	-209.2 ± 5.8	-283.3 ± 25	-191.3 ± 17
standard uncertainty of fit	0.5	0.6	1.8
MVFT1, eq 10			
<i>a</i> '	-3.1947 ± 0.030	-3.5077 ± 0.054	-2.654 ± 0.13
<i>b</i> ' × 10 ³ /MPa ⁻¹	-1.2181 ± 0.079	0.0742 ± 0.373	-2.323 ± 0.32
<i>c</i> '/K	1291.0 ± 9.2	1423.6 ± 16.4	1121 ± 37
<i>d</i> '/(K·MPa ⁻¹)	1.991 ± 0.013	2.090 ± 0.057	2.269 ± 0.067
<i>e</i> ' × 10 ⁵ /(K·MPa ⁻²)	-105.68 ± 2.7	-125.07 ± 10.0	-94.45 ± 8.3
<i>T</i> ₀ /K	155.10 ± 0.54	157.20 ± 0.86	162.2 ± 2.4
standard uncertainty of fit	0.5	0.5	1.8
MVFT2, eq 11			
<i>a</i> ''	-3.234 ± 0.032	-3.4431 ± 0.057	-2.975 ± 0.14
<i>b</i> '' × 10 ³ /MPa ⁻¹	2.586 ± 0.054	4.083 ± 0.256	2.521 ± 0.25
<i>D</i>	8.448 ± 0.094	8.874 ± 0.16	7.802 ± 0.41
<i>x</i> /K	154.322 ± 0.56	158.21 ± 0.91	156.17 ± 2.69
<i>y</i> × 10 ² /(K·MPa ⁻¹)	8.211 ± 0.058	8.062 ± 0.24	9.971 ± 0.24
<i>z</i> × 10 ⁵ /(K·MPa ⁻²)	-8.568 ± 0.23	-9.634 ± 0.50	-9.74 ± 0.89
standard uncertainty of fit	0.5	0.6	1.8

^a ML and MVFT1 coefficients for [BMIM]PF₆ from ref 2 are included for comparison.

The negative offsets of the results of the Brennecke group^{7,10} are consistent with the reported mass fractions of water in their second paper,⁷ 0.0046 and 0.0024 respectively, or mole fractions 0.0675 and 0.0435. Based on our results, ideal solutions of these compositions would have densities of (1.0965 and 1.2264) g·cm⁻³ respectively at 25 °C. Their values are (1.0912 and 1.2245) g·cm⁻³. For [OMIM]BF₄, there is good agreement with the results of Seddon et al.,¹¹ who used a much drier sample (35·10⁻⁶ mass fraction) than the Brennecke group: there is excellent agreement at 25 °C between our result, 1.10368 g·cm⁻³, and that of Heintz et al.,¹³ 1.10381 g·cm⁻³. For [OMIM]-PF₆, there is very good agreement with the single 25 °C vibrating-tube point of Dzyuba and Bartsch.¹⁴ The pycnometric results of Seddon et al.¹¹ deviate from ours in this case, but their sample contains slightly more water than ours, 80·10⁻⁶ mass fraction.

The viscosities are presented in Table 5 and 6. As there are no high-pressure data in the literature, comparison with the results of other workers^{11,15} is confined to atmospheric pressure. As for [BMIM]PF₆,² the data were fitted to the Litovitz equation:¹⁶

$$\eta = A \exp(B/RT^3) \quad (7)$$

which has the advantages of (a) containing only two fitted parameters and (b) being ideal for extrapolation, as well as the more commonly used Vogel–Fulcher–Tammann (VFT) equation:

$$\eta = A' \exp(B'/(T - T_0)) \quad (8)$$

The coefficients are given in Table 7. Angell¹⁷ has developed a global classification of liquids based on eq 8. His strength parameter *D* ($\equiv B'/T_0$) is large for “strong” liquids where the viscosity approaches an Arrhenius (Andrade) temperature dependence and is small for “fragile” liquids. A number of workers have commented on the need for care in fitting data to the VFT equation.¹⁸ We have employed AXUM graphics software (Mathsoft Inc.) which uses the Levenberg–Marquardt nonlinear least-squares algorithm¹⁹ recommended by Mano and

Pereira,¹⁸ fitting $\ln \eta$, but weighting the data to allow for choosing this form ($w \propto 1/\eta$) and, as well, in proportion to the percentage experimental error ($w \propto \eta$). These two weightings conveniently cancel.

Figure 3 shows the deviations of our results and the literature data from these equations. When expanded to a larger scale, the residual plots show some systematic trends at the temperature extremes, but these are within the overall experimental uncertainty. The results of Seddon et al.¹¹ agree well with ours at higher temperatures but tend to be much lower at lower temperatures, whereas for [BMIM]PF₆ the results from our two groups are in better accord over the whole temperature range.² The results of Branco et al.¹⁵ are also much lower, particularly for [OMIM]BF₄, where they are about one-third of our values. Both these data sets were obtained with cone and plate viscometers, the Branco instrument being open to the laboratory atmosphere.²⁰

The general form of the pressure dependence of the shear viscosity of liquids is greater than exponential at moderate pressures [$(\partial \ln \eta / \partial p)_T < 0$] and less than exponential at very high pressures [$(\partial \ln \eta / \partial p)_T > 0$], typically above 0.5 GPa.^{21,22} Consequently, as for [BMIM]PF₆,² we have used modified Litovitz (ML) and VTF (MVFT1) equations to fit the data set as a whole:

$$\eta = \exp(a + bp + (c + dp + ep^2)/T^3) \quad (9)$$

$$\eta = \exp(a' + b'p + (c' + d'p + e'p^2)/(T - T_0)) \quad (10)$$

The quality of the fits for the two equations is very similar: coefficients are given in Table 8. The modified VFT equation yields a pressure-dependent strength parameter, $D = (c' + d'p + e'p^2)/T_0$. This is plotted as a function of pressure in Figure 5 where values for [BMIM]PF₆ are also included. *D* increases in the order [BMIM]PF₆ < [OMIM]BF₄ < [OMIM]PF₆; that is, [BMIM]PF₆ is the most fragile. *D* increases with increasing pressure in each case.

It has been argued that *D* should be independent of pressure, at least in some cases.^{23,24} This then requires that *T*₀ be pressure-

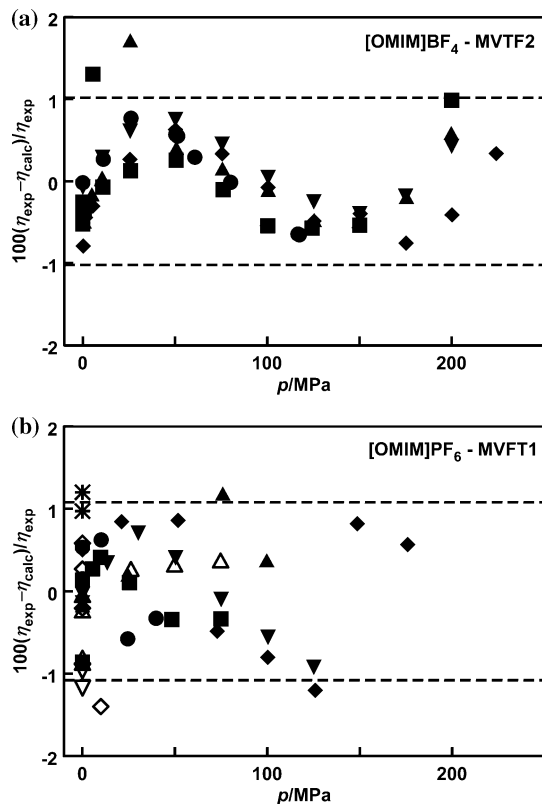


Figure 4. (a) Residuals (experimental – calculated values) for the fit of the experimental viscosities for [OMIM]BF₄ to eq 11 (MVFT2) as a function of temperature and pressure, p . Symbols: ●, 25 °C; ■, 35 °C; ▲, 50 °C; ▼, 60 °C; ◆, 75 °C. (b) Residuals (experimental – calculated values) for the fit of the experimental viscosities for [OMIM]PF₆ to eq 10 (MVFT1) as a function of temperature and pressure, p . Symbols: sample OP1 —, △, 50 °C; ▽, 60 °C; ◇, 70 °C; *80 °C; sample OP2 —, ●, 25 °C; ■, 35 °C; ▲, 50 °C; ▼, 60 °C; ◆, 70 °C.

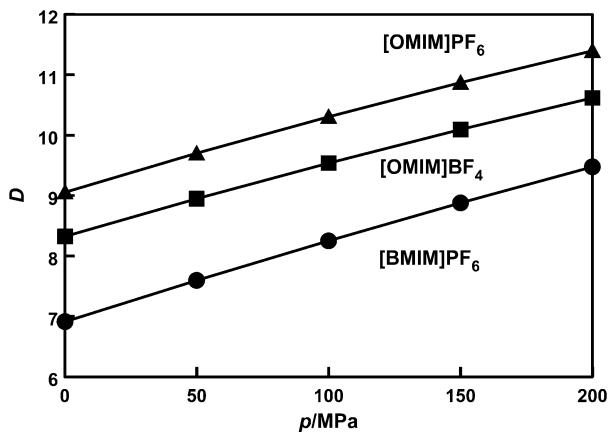


Figure 5. Pressure dependence of the Angell strength parameter D , obtained from the parameters of eq 10. Symbols: ●, [BMIM]PF₆; ■, [OMIM]BF₄; ▲, [OMIM]PF₆.

dependent, and it should increase with increasing pressure like the glass transition temperature, T_g . Accordingly, our results have also been fitted to the equation (MVFT2):

$$\eta = \exp(a'' + b''p + DT_0(p)/(T - T_0))$$

$$T_0(p) = x + yp + zp^2 \quad (11)$$

The quality of the fit is little changed (Table 8 and Figure 4), but this is not surprising given that the number of fitted coefficients is unchanged. (It should be noted that the parameters

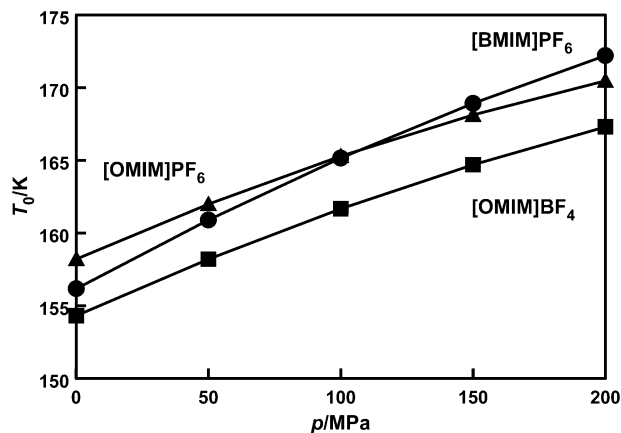


Figure 6. Pressure dependence of the VFT parameter T_0 , obtained from the parameters of eq 11. Symbols are the same as for Figure 5.

Table 9. Test of the Angell Relationship between D , T_0 , and T_g

	[OMIM]BF ₄	[OMIM]PF ₆	[BMIM]PF ₆
Parameters from VFT, eq 8			
T_0 /K	155.5	158.0	161.8
D	8.25	8.91	6.96
T_g /K ^a	193.7	191.2	197.1
T_g/T_0	1.25	1.21	1.22
T_g/T_0 from eq 12	1.21	1.23	1.18
Parameters from MVFT2, eq 11			
$T_0(=x)$ /K	154.3	158.2	156.2
D	8.45	8.87	7.80
T_g/T_0	1.26	1.21	1.26
T_g/T_0 from eq 12	1.22	1.23	1.20

^a Glass temperatures: [OMIM]BF₄, ref 26; [OMIM]PF₆, ref 9; [BMIM]PF₆, ref 27.

b' and b'' in eqs 10 and 11 seem to be necessary for an adequate fit.) Figure 6 shows that (dT_0/dp) is indeed positive, although it decreases slightly with increasing pressure. T_0 values for the two hexafluorophosphate salts are essentially equal within the error of the fits, with T_0 for [OMIM]BF₄ being slightly lower.

Angell²⁵ has suggested the following relationship between D , T_0 , and the glass temperature T_g , based on the scaling of the (coexistence line) viscosities of a wide range of liquids in the range $0 < (T_g/T_0) < 1$, with the assumption of a common single viscosity value (η_g) at T_g . Thus

$$T_g/T_0 = 1 + D/(2.303 \log(\eta_g/\eta_0)) \quad (12)$$

η_0 is A' of the VFT equation (eq 8). Angell found $\log(\eta_g/\eta_0)$ empirically to be about 17. The values of D and T_0 derived from VFT and MVFT2 and experimental T_g values from the literature are found to be consistent with Angell's relationship (Table 9).

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